

## A2D Cubic Functions with Irrational and Complex Solutions

Name \_\_\_\_\_

- Use your grapher to find the INTEGER zero(s).
- Use synthetic division to break down the polynomial to find a quadratic result.
- Then solve your quotient to find the remaining zeros (exact values).
- State the total number of zeros, and list which ones are Integer vs irrational.
- Write  $f(x)$  in x-intercept (factored) form.

1.  $f(x) = x^3 - 4x^2 - 2x + 8$

2.  $f(x) = x^3 - 8x - 8$

Solutions:

Integer:

Irrational:

Complex:

3.  $f(x) = x^3 - 3x^2 - 2x + 6$

4.  $f(x) = x^3 + 5x^2 - 7x - 35$

Solutions:

Integer:

Irrational:

Complex:

5.  $f(x) = x^3 + 3x^2 + 4x + 12$

6.  $f(x) = x^3 - 5x^2 + 36x - 180$

Solutions:

Integer:

Irrational:

Complex

7. Use a graphing calculator to find an integer zero, and then use the Quadratic Formula to find all the remaining roots.

$$f(x) = x^3 - 12x^2 + 54x - 68$$

Roots:

Equation in Factored Form:

Problems 8-9: Use the zeros of the polynomial to write an equation in factored form. Then write it in expanded form.

8. Zeros of  $f(x)$ :  $-3, i, -i$

9. Zeros of  $f(x)$ :  $2, \pm \sqrt{5}$

11. Find the missing factors:  $2x^3 + 3x^2 - 3x - 2 = (x + 2)(\quad)(\quad)$

12. Divide using long division.  $(x^5 + 3x^3 + x^2 - 10x + 6) \div (x^2 + 5)$

13. Solve the following equation for L:  $T = 2\pi\sqrt{\frac{L}{g}}$

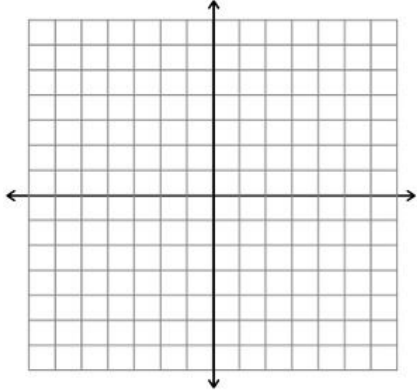
14. Simplify:  
 $(3 - 5i)(2i + 5) - (-4 + 6i)$

15. Given that there is a zero at -5 in  $P(x) = x^3 + 9x^2 - 1x - 105$ .  
Use synthetic division to prove that -5 is a zero. Then factor and write as a product of linear factors.

$P(x) = (x \text{ \_\_\_\_\_\_})(x \text{ \_\_\_\_\_\_})(x \text{ \_\_\_\_\_\_})$

Zeros are \\_\\_\\_\\_\\_\\_, \\_\\_\\_\\_\\_\\_, \\_\\_\\_\\_\\_\\_

Graph without a calculator #13. Make sure you LABEL the x & y Intercepts.



16. Find the quadratic with zero at -7i?

17. Complete the Table for the 2 options for Cubic Polynomials:

Real Solutions	Complex Solutions